

Q1) Find the HCF of $2n + 13$ and $n + 7$, where n is a natural number.

- 1) 1 2) $n + 6$ 3) $n + 7$ 4) Depends on n

As 'n' is a natural number so, substitute any natural number in place of n.

Put $n = 1$. HCF of $2n + 13$ and $n + 7 =$ HCF of 15 and 8 = 1

When $n = 1$, then option 2 and 3 are eliminated. So, answer is either option 1 or option 4.

Now, put another value of n. Say $n = 2$. HCF of $2n + 13$ and $n + 7 =$ HCF of 17 and 9 = 1

As the answer does not depend on the value of 'n' so, option 1 is the answer.

Q2) If $\frac{a}{b} = \frac{1}{3}, \frac{b}{c} = 2, \frac{c}{d} = \frac{1}{2}, \frac{d}{e} = 3, \frac{e}{f} = \frac{1}{4}$, then what is the value of $\frac{abc}{def}$.

- 1) $3/8$ 2) $27/8$ 3) $1/4$ 4) $27/4$

$$\frac{a}{b} = \frac{1}{3} = \frac{2}{6}, \frac{b}{c} = 2 = \frac{6}{3}, \frac{c}{d} = \frac{1}{2} = \frac{3}{6}, \frac{d}{e} = 3 = \frac{6}{2}, \frac{e}{f} = \frac{1}{4} = \frac{2}{8}$$

So, $a = 2, b = 6, c = 3, d = 6, e = 2, f = 8$ i.e. $\frac{abc}{def} = \frac{3}{8}$

Q3) If $a + b + c = 0$ the value of $\frac{a^4 + b^4 + c^4}{a^2b^2 + b^2c^2 + c^2a^2}$ is

- 1) 2 2) 3 3) 4 4) 5

In this question, $a + b + c = 0$.

Put $a = 1, b = 0$ so $c = -1$

$$\frac{a^4 + b^4 + c^4}{a^2b^2 + b^2c^2 + c^2a^2} = \frac{1 + 0 + 1}{1} = 2$$

Q4) If $x = a^2 - bc, y = b^2 - ca$ and $z = c^2 - ab$, then the value of

$\frac{(a+b+c)(x+y+z)}{ax+by+cz}$ is

- 1) 3 2) 2 3) 1 4) 0

Say $a = 1, b = 2, c = 0$

Then $x = 1, y = 4$ and $z = -2$

$$\frac{(a + b + c)(x + y + z)}{ax + by + cz} = \frac{(1 + 2 + 0)(1 + 4 - 2)}{1 + 8} = \frac{3 \times 3}{9} = 1$$

Q5) If $a + b + c = 3$, $a^2 + b^2 + c^2 = 5$ and $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 1$ where a, b, c are non-zero, then the value of abc is

- 1) 1 2) $\frac{3}{4}$ 3) $\frac{3}{2}$ 4) 2

In this question, we have 3 conditions. So, whenever we have multiple conditions then we need to follow full method

$$(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$$

$$9 = 5 + 2(ab+bc+ca) \text{ i.e. } ab+bc+ca = 2$$

Dividing both sides by abc we get, $\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = \frac{2}{abc} = 1$

So, $abc = 2$

Q6) If $a + b + c = 0$ then one of the roots of the equation $ax^2 - bx + c = 0$ is

- 1) $-\frac{c}{a}$ 2) $\frac{c}{a}$ 3) $\frac{b-a}{a}$ 4) $\frac{b}{a}$

In this question, $a + b + c = 0$

Put $a = 1, b = 2$ so, $c = -3$. The equation becomes $x^2 - 2x - 3 = 0$

On solving, $x = -1, 3$

Option 1: $-\frac{c}{a} = 3$ (Possible)

As we are using substitution method so we need to check other options also.

Option 2: $\frac{c}{a} = -3$ (Not Possible)

Option 3: $\frac{b-a}{a} = 1$ (Not Possible)

Option 4: $\frac{b}{a} = 2$ (Not Possible)

Q7) If $ab + bc + ca = 0$ then the value of $\frac{1}{a^2-bc} + \frac{1}{b^2-ca} + \frac{1}{c^2-ab}$ is

- 1) 3 2) $3abc$ 3) abc 4) 0

In this question, $ab + bc + ca = 0$

Put $a = 1 = b$ then $c = -\frac{1}{2}$

$$\frac{1}{a^2 - bc} + \frac{1}{b^2 - ca} + \frac{1}{c^2 - ab} = 0$$

Q8) If $x = a + \sqrt{a^2 - 1}$ then $x^3 + \frac{1}{x^3}$ is equal to

- 1) $3a^3 - 3a$ 2) $8a^3 - 6a$ 3) $8a^3 + 6a$ 4) $3a^3 + 3a$

Put $a = 1$ then $x = 1$

$$x^3 + \frac{1}{x^3} = 2$$

Put $a = 1$ in options. Option 2 gives the answer as '2'.

Q9) Find the sum of 'n' terms in the series $7+77+777+7777+\dots$ n terms

- 1) $\frac{7}{81}(10^{n+1} - 9n + 10)$ 2) $\frac{7}{81}(10^{n+1} - 9n - 10)$
 3) $\frac{7}{9}(10^{n+1} - 9n - 10)$ 4) $\frac{7}{9}(10^{n+1} - 9n + 10)$

Put $n = 1$ i.e. sum of 1 term of the series. So, required answer is 7.

Put $n = 1$ in options.

Option 1: $\frac{7}{81}(10^{n+1} - 9n + 10) = \frac{707}{81}$

Option 2: $\frac{7}{81}(10^{n+1} - 9n - 10) = 7$

Option 3: $\frac{7}{9}(10^{n+1} - 9n - 10) = 63$

Option 4: $\frac{7}{9}(10^{n+1} - 9n + 10) = \frac{707}{9}$

Hence, option 2 is the answer.

Q10) Find the value of $4 \log x + 4 \log x^{2 \times 2} + 4 \log x^{3 \times 3} \dots \dots + 4 \log x^{k \times k}$

- 1) $\frac{(k^2+k)(2k+1)}{6}$ 2) $\frac{k(k+1)}{6}$ 3) $(k - 1) \log x$
 4) $\frac{2}{3}(k^2 + k)(2k + 1) \log x$

Put $k = 1$

$4 \log x + 4 \log x^{2 \times 2} + 4 \log x^{3 \times 3} \dots \dots + 4 \log x^{k \times k} = 4 \log x \{ \text{when } k = 1 \}$

Put $k = 1$ in options. Option 4, gives the answer as '4 log x'

Q11) What is the sum of 'n' terms in the series

$$\log m + \log \left(\frac{m^2}{n}\right) + \log \left(\frac{m^3}{n^2}\right) + \log \left(\frac{m^4}{n^3}\right) + \dots \dots \dots ?$$

1) $\log \left[\frac{n^{n-1}}{m^{n+1}}\right]^{\frac{n}{2}}$ 2) $\log \left[\frac{m^m}{n^n}\right]^{\frac{n}{2}}$ 3) $\log \left[\frac{m^{1-n}}{n^{1-m}}\right]^{\frac{n}{2}}$ 4) $\log \left[\frac{m^{n+1}}{n^{n-1}}\right]^{\frac{n}{2}}$

Put $n = 1$ i.e. sum of 1 term of the series. So, required answer is $\log m$. Put $n = 1$ in options. Option 4 gives the result as $\log m$.

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